

St Francis of Assisi Progression in calculation Policy

At St Francis of Assisi, Christ is at the centre and the children are at the heart of our whole school learning community in pursuit of excellence in all aspects of school life. We work collaboratively to identify and harness potential to be the very best that we can be. We maximise opportunities for all in order to acquire essential life skills and reach our full potential as global citizens.

September 2023

Before children move to written methods, they need:

- To understand the number system
- Know some number facts
- Have good mental strategies / mental agility!
- Be confident use concrete apparatus and pictorial representations to solve problems and explain their reasoning.

When children move to written methods they need to think...

- What will the answer be roughly?
- Can I work it out in my head?
- What can I use to help me? Do I need a written method?
- Does that answer my question?
- Does it make sense? Can I check?

Purpose of the Policy:

- To make teachers and parents aware of the strategies that pupils are formally taught within each year group that will support them to perform mental and written calculations. Pupils should not move on through the methods until they have secured and understood how to use the methods, including the concrete and pictorial representations.
- The policy supports teachers in identifying appropriate concrete apparatus and pictorial representations to help develop and secure understanding.

Aims of the policy:

- To ensure consistency and progression in our approach to calculation.
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations.
- To ensure that children can use these methods accurately with confidence and understanding.

How to use this policy:

- Use the policy as the basis of your planning but ensure you use previous or following years' guidance to allow for personalised learning.
- Always use Assessment for Learning to identify suitable next steps in calculation for groups of children.
- If, at any time, children are making significant errors, return to the previous stage in calculation.
- Always introduce a new concept/calculation using use suitable resources, models and images to support children's understanding of the calculation and place value, as appropriate.
- Encourage children to make sensible choices about the methods they use when solving problems.



Add Plus Total	+ Addition +	More Sum	Altogether
Year 3 Method to be used by core of class	Year 4 Method to be used by core of class	Year 5 Method to be used by core of class	Year 6 Method to be used by core of class
As year 2 plus: Understand place value - can partition numbers & recombine numbers to support column addition. 200 20 20 2 200 20 20 20 2 200 20 20 20 20 200 20 20 20 20 20 200 20 20 20 20 20 20 200 20 20 20 20 20 20 20 20 20 200 20 20 20 20 20 20 20 20 20 20 20 20	As year 3 plus: Add ones, tens, hundreds and thousands to a four-digit number Children can draw a pictoral representation of the columns and place value counters to further support their learning and understandina. Compact addition (integers only) with numbers up to four digits e.g. 7648 ± 1486 <u>9134</u> 111 Expanded addition may be used for decimals in real contexts e.g. money and length. £11.35+ £12.43= £10 + £1 + 30p + 5p + <u>£10 + £2 + 40p + 3p</u> <u>£20 + £3 + 70p + 8p</u> = £23.78	As year 4 plus: Compact addition with numbers larger than four digits. Compact addition with decimals to two places. e.g. $ \begin{array}{r} 32.75 \\ $	As year 5 plus: Compact addition involving large numbers. Compact addition with decimals to three places. e.g. 32.756 +48.646 <u>81.402</u> 11 11 24.5+ 36.238 24.500 + <u>36.238</u> <u>60.738</u> 1
See addition appendix 5 column method- no regrouping and appendix 6 column method – regrouping (bridging ten)	See addition appendix 5 column method- no regrouping and appendix 6 column method – regrouping (bridging ten)	See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)	See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)



Subtract take away less t	han - Subtraction	- minus differer.	oce between
Year 3 Method to be used by core of class	Year 4 Method to be used by core of class	Year 5 Method to be used by core of class	Year 6 Method to be used by core of class
As year 2 plus: 13 - 7 = 6 3 4 -3 -3 -3 -3 -3 -3 -3 -3 -3 -3	As year 3 plus: Subtract ones, tens, hundreds, and thousands from a four-digit number. Number line method (2, 3, 4 digit numbers, extending to decimals in a real context) e.g. $43\cdot21 - 41\cdot65 = 41\cdot56$ $+5p + 20p + 61 \circ 0 + 21p$ Expanded subtraction e.g. 354 - 165	As year 4 plus: Compact subtraction, involving numbers larger than 4 digits and with decimals to 2 places. Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident children can find their own way to record the exchange/regrouping.	As year 5 plus: Compact subtraction involving large numbers. Compact subtraction with decimals up to three places. 22:27 - 12:88 10:49
351 - 165 = 186 $45 + 100 + 50 + 11$ $165 = 170 200 300 350 351$ Begin expanded subtraction using concrete objects and pictorial representations. 48.7 $10s 1s$ 48.7 $10s 1s$ 48.7 $10s 1s$	$\frac{200}{300} + \frac{140}{50} + \frac{1}{1}$ $\frac{100}{100} + \frac{60}{50} + \frac{5}{5}$ $100 + 80 + 6 = 186$ $\frac{176 - 64 = 1}{176}$ $\frac{176}{-\frac{64}{112}}$ Use base 10 or place value counters alongside the written calculation to help to show working.	Image: system Image: system Image: system	cleck 10.49 + 12.88 23.37
Start to use Compact subtraction.Not RegroupingRegrouping44-741-741-2Show the carrying at the top as above.See subtraction appendix 5 make 10. Appendix 6column method without regrouping.	Compact subtraction (regrouping) 23'5'1 - 165 186 See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.	See Appendix 7 column method with regrouping.	See Appendix 7 column method with regrouping.

Multiply times lots	of × Multiplication × groups	of multiple of product
Year R	Year 1	Year 2
Method to be used by core of class	Method to be used by core of class	Method to be used by core of class
Introduce language and concept of making equal groups. Begin to double numbers to 5. Use concrete apparatus to show how to double a number.	As year R plus: Recall doubles to 10. Use this knowledge to support halving and doubling larger numbers.	As Year 1 plus: By the end of the year pupils should recall all multiplication facts for the 2, 5 and 10 times tables.
Double 4 is 8	half of 8 is 4 8+2=4 double 4 is 8 $4\times 2=8$	Understand multiplication is about equal groups and use arrays to show this. Also be able to use these arrays to show and understand that multiplication is commutative. $4 \times 2 = 8$
	Understand multiplication as repeated addition.	2 × 4 = 8
See multiplication appendix 1 doubling.	5+5+5+5+5=30 $5\times 6=30$ 5 multiplied by 6 6 groups of 5	
	6 hops of 5	Understand multiplication as scaling.
	2+2+2+2=10	The giant is twice as big as a boy.
	Group sets of objects reliably in 2s, 5s and 10s. There are groups of pencils.	Understand that multiplication and division are the inverse of each other.
	Go Go Go There are groups of flowers	4×10=40
		10×4=40
		40÷4=10
		40÷10=4
	Recognise number sequences e.g. 2s, 5s and 10s.	See multiplication appendix 2 counting in multiples. Appendix 3
	See multiplication appendix 1 doubling. Appendix 2 counting in multiples. Appendix 3 repeated addition. Appendix 4 arrays-showing commutative multiplication.	repeated addition. Appendix 4 arrays- showing commutative multiplication.

Multiply times	lots of × Multiplica	tion × groups of mult	iple of product
Year 3	Year 4	Year 5	Year 6
Method to be used by core of class	Method to be used by core of class	Method to be used by core of class	Method to be used by core of class
As year 2 plus:	As year 3 plus:	As year 4 plus:	As year 5 plus:
Focus on understanding, representing and	ALL times tables facts to 12 x 12 should	Bar modelling and number lines can support	Long Multiplication
remembering times tables facts for 2,5,10,3,4	be known by end of year 4 including	learners when solving problems with	Up to 4 digit x 2 digit
and 8 times tables, including division facts	multiplying by 0 and 1.	multiplication alongside the formal written	
0000000	Children should learn to multiply three	method.	0.5
e.g	numbers together.	59 59 59 59 59 59 59 69 69	35
<u>ଭ ଭ ଭ ଭ ଭ ଭ ଭ</u> ଭ	$4 \times 6 \times 3 =$		<u>x+6</u> 2+0
ବିବିବିବିବିବିବିବି	4 x 6= 24 x 3= 72	8 × 59	111-30
4x8=32 8x4=32 32÷4=8 32÷8=4	Grid method TU X U or HTU X U	8 *6 = 48	1700
	This can be used to help children	8 × 60 = 480	1610
Understand that multiplication is repeated	understand exactly what you are	480 - 8 - (4/2)	
addition e.g. 3x4 = 4+4+4. Use concrete,	multiplying.		
pictorial and abstract methods	e.g. 245 x 6	Short multiplication - up to four digits by	Moving to Decimal numbers to 2 places
	x 200 40 5 Tot	one digit	multiplied by whole numbers
	al	2741 × 6 becomes	
44 44 44	6 120 24 30 147	2 7 4 1	Note -some children may continue to use the
88 88 88	0 0 0	× 6	grid method
	Partitioning	Answer: 16 446	If it helps, children can write out what they
į	4 × 15		are solving next to their answer.
Expanded Column & Compact Column Methods	10 5	Long Multiplication – four digits by two digits	22
	10 × 4 = 40	Use expanded to help understanding if	x 24
H T O H T O	5 × 4 = 20 40 + 20 = 60	needed then move onto compact.	$\frac{1}{8}$ (4 x 2)
x 5 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7		Expanded Compact	120 (4 x 30)
+ 1 5 0 (5×30) 1 7 0	Short Multiplication	35 35	40 (20 x 2)
	6 x 25 =	$\frac{\times 46}{30}$	<u>600</u> (20 x 30)
Note - before moving to any TU x U, the	23	$\frac{1400}{100}$	768
children will need be able to multiply a	<u>× 6</u>	<u>1610</u>	
multiple of 10 by a single digit	138		
	1 1 Show the carrying below		See multiplication appendix 1 append
See multiplication appendix 4 arrays- showing	See multiplication appendix 4 arrays-	See multiplication appendix 4 arrays- showing	showing commutative multiplication Appendix
commutative multiplication. Appendix 5 grid	showing commutative multiplication	commutative multiplication. Appendix 5 grid	5 arid method. Appendix 6 column
method.	Appendix 5 grid method.	method. Appendix 6 column multiplication.	multiplication.



Share equally group equa	elly divide ÷ Divisi	on ÷ remainder fac	tor quotient
Year 3	Year 4	Year 5	Year 6
Agreed method to be used by core of class	Agreed method to be used by core of class	Agreed method to be used by core of class	Agreed method to be used by core of class
As year 2 plus:	As year 3 plus:	As year 4 plus:	As year 5 plus:
Focus on understanding, representing and	Focus on understanding, representing and	Short division, up to 4 digit numbers	Short division, up to 4 digit numbers divided
remembering times tables facts for 2,5,10,3,4	remembering times tables facts for ALL	divided by 1 digit numbers	by 1 or 2 digit numbers
and 8 times tables, including division facts.	times tables up to 12 x12 including division	e.g 4251÷3	e.g. 423 ÷ 18
eg & & & & & & & & & & & & & & & & & & &	facts. It is especially important that children understand that division can be grouping or sharing.	3 [4'2.5']	18 423:0
121 121 121 121 121 121 121 121 121		Including dealing with remainders in	or Long division
	e.g. 12÷3=4	context.	
4x8=32. 8x4=32, 32÷4=8, 32÷8=4	12 sweets between 3 people gives 4 sweets each.	326 R6	23.5
Use number lines to support repeated subtraction. '3 groups of 4, with 1 left over'		7 22 88	- <u>36</u> 63 <u>54</u> 90
		able children.	
6 I I I I I I I I I I I I I I I I I I I	(3 groups of 4) 'How many 3s in 12?' gives 4 groups of 3	e.g. $150 \div 8 = 18 R 6$ 10×8 5×8 3×8 R6 30 120 144 150 (How many 8s) (How many 8s) (How to help me?	
See division appendix 3 division within arrays. Appendix 4 division with a remainder.	See division appendix 3 division within arrays. Appendix 4 division with a remainder.	Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000. See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division.	See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division, Appendix 6 long division.

Appendix

Progression in calculations linked to concrete apparatus, pictorial representations and abstract methods. When introducing a new method of calculation the concrete apparatus should be used first. Once this is secure pupils can then be moved onto pictorial representations and then abstract methods.

Addition:

Objective and	Concrete	Pictorial	Abstract
Strategies			
Appendix 1- Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar.	yart yart	4 + 3 = 7 10= 6 + 4 5 Use the part-part whole diagram as shown above to move into the abstract.
Appendix 2- Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 10 11 12 13 14 15 16 17 18 19 20 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.

Appendix 3- Regrouping to make 10.	6 + 5 = 11	Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
	Start with the bigger number and use the smaller number to make 10.	9 + 5 = 14 $1 4$ $+1$ $+1$ $+4$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$	
Appendix 4- Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Image:	+ + + + + + + + + + + + + + + + + + +	4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
Appendix 5- Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.	$\frac{Calculations}{21 + 42} =$
			21 + <u>42</u>



Subtraction:

Objective and Strategies	Concrete	Pictorial	Abstract
Appendix 1- Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. 6 - 2 = 4	Cross out drawn objects to show what has been taken away. $ \begin{array}{c} $	18 -3= 15 8 - 2 = 6
Appendix 2- Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 -10 -10 -10 -10	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

Appendix 3- Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the difference Use basic bar models with items to find the difference	+6 Count on to find the difference. Count on to find the difference. Count on to find the difference. Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 Sister 22	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.
Appendix 4 Part- Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	5 10 Move to using numbers within the part whole model.
Appendix 5- Make 10	14 - 9 = Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 5 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 - 8= How many do we take off to reach the next 10? How many do we have left to take off?





Multiplication

Objective and	Concrete	Pictorial	Abstract
Strategies			
Appendix 1- Doubling	Use practical activities to show how to double a number. double 4 is 8 4×2=8	Draw pictures to show how to double a number. Double 4 is 8	16 10 10 10 10 10 10 10 10 10 10
Appendix 2- Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25 , 30

Appendix 3- Repeated addition		There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $ $ \begin{array}{c} \end{array} $ $ \end{array} $	Write addition sentences to describe objects and pictures.
	Use different objects to add equal groups.	5 5 5 5 5 5 5 5 5 5 5 5 5 5	2+2+2+2=10
Appendix 4-	Create arrays using counters/ cubes to show	Draw arrays in different rotations to	Use an array to write
commutative multiplication		sentences. Sentences. $4 \times 2 = 8$ $2 \times 4 = 8$ $4 \times 2 = 8$ Link arrays to area of rectangles.	reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 $5 \times 3 = 15$ $3 \times 5 = 15$

Appendix 5-Grid Method

Show the link with arrays to first introduce the grid method.



Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

210 + 35 = 245

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

	10	8
10	100	80
3	30	24

Х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Appendix 6-Column multiplication Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.





Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.

32 × 24 8 120 40 600	(4 x 2) (4 x 3) (20 x 2) (20 x 3)) 0) 2) 30)				
768					7	4
			×		6	3
					1	2
				2	1	0
				2	4	0
		+	4	2	0	0
			4	6	6	2
This mo method	oves to [.]	the	mor	e co	omp	act

Division

Objective and Strategies	Concrete	Pictorial	Abstract
Appendix 1- Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. Children use pictures or shapes to share quantities. 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 +	Share 9 buns between three people. 9 ÷ 3 = 3
Appendix 2- Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

		96 ÷ 3 = 32	Think of the bar a are dividing by and	as a whole. Split it i d work out how man 20 20 20 ÷ 5 = ? 5 x ? = 20	nto the num y would be v	ber of groups you within each group.	
Appendix 3- Division within arrays	Image: constraint of the sector of the se	Link division to multiplication by creating an array and thinking about the number sentences that	Draw an array and mul	Image: Constraint of the second se	() () () () () () () () () () () () () (to groups to make	Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7
Appendix 4- Division with a remainder	14 ÷ 3 = Divide objects betwee much is left over	en groups and see how	Jump forward in e more you need to	equal jumps on a nur jump to find a remo 4	nber line the ainder.	en see how many	Complete written divisions and show the remainder using r. $29 \div 8 = 3$ REMAINDER 5 $\uparrow \uparrow \uparrow \uparrow$ dividend divisor quotient remainder

		Draw dots and group them to divide an amount and clearly show a remainder.	
Appendix 5- Short division	Tens Units 3 2 3 0 0 0 3 0 0 0 0 3 0 0 0 0 4 0 0 0 0 42 ÷ 3 0 0 0 0	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder. Move onto divisions with a 2 1 8 8 6 r 2 3 5 4 3 2 remainder.
	42 ÷ 3= Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.		Finally move into decimal places to divide the total accurately. 1 4 . 6 16 21 3 5 5 1 1 . 0

