



St Francis of Assisi

Progression in calculation Policy

At St Francis of Assisi, Christ is at the centre and the children are at the heart of our whole school learning community in pursuit of excellence in all aspects of school life. We work collaboratively to identify and harness potential to be the very best that we can be. We maximise opportunities for all in order to acquire essential life skills and reach our full potential as global citizens.

June 2025

Before children move to written methods, they need:

- To understand the number system
- Know some number facts
- Have good mental strategies / mental agility!
- Be confident use concrete apparatus and pictorial representations to solve problems and explain their reasoning.

When children move to written methods they need to think...

- What will the answer be roughly?
- Can I work it out in my head?
- What can I use to help me? Do I need a written method?
- Does that answer my question?
- Does it make sense? Can I check?

Purpose of the Policy:

- To make teachers and parents aware of the strategies that pupils are formally taught within each year group that will support them to perform mental and written calculations. Pupils should not move on through the methods until they have secured and understood how to use the methods, including the concrete and pictorial representations.
- The policy supports teachers in identifying appropriate concrete apparatus and pictorial representations to help develop and secure understanding.

Aims of the policy:

- To ensure consistency and progression in our approach to calculation.
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations.
- To ensure that children can use these methods accurately with confidence and understanding.

How to use this policy:

- Use the policy as the basis of your planning but ensure you use previous or following years' guidance to allow for personalised learning.
- Always use Assessment for Learning to identify suitable next steps in calculation for groups of children.
- If, at any time, children are making significant errors, return to the previous stage in calculation.
- Always introduce a new concept/calculation using use suitable resources, models and images to support children's understanding of the calculation and place value, as appropriate.
- Encourage children to make sensible choices about the methods they use when solving problems.

Add Plus Total

+ Addition +

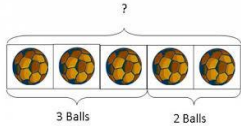
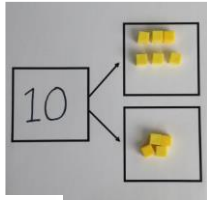
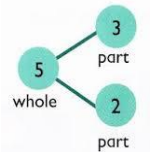
More Sum Altogether

Year R

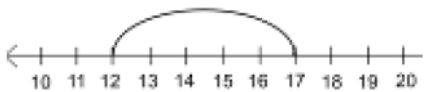
Method to be used by core of class



Use pictures, tens frames, cubes and other concrete resources to add two numbers together as a group or in a bar.



Children to prepare to add and subtract on a number line by counting on and back.



See addition appendix 1- combining two parts to make a whole: part-whole model.

Year 1

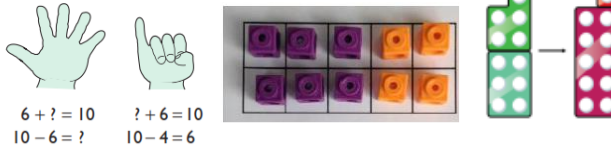
Method to be used by core of class

As year R plus:

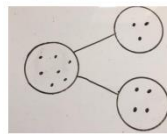
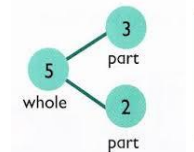
Teach all the number bonds up to and including 10 and the related 'Fact Family' for each fact.

$$10 = 6 + 4 \quad 4 + 6 = 10$$

$$10 - 4 = 6 \quad 10 - 6 = 4$$



Use concrete objects to combine groups to add and solve missing number problems.

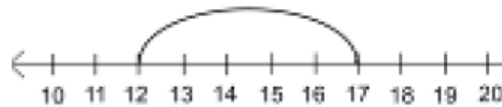


$2 + _ = 5$ Show this using the part/whole model.

Understand place value - can partition numbers and recombine numbers



Usually start with the **biggest** number (if counting on)
 $12 + 5 = 17$



Start at the larger number on the number line and count on in ones or in one jump to find the answer.

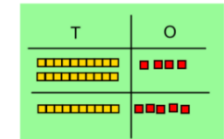
See addition appendix 1- combining two parts to make a whole: part-whole model. Appendix 2 starting at the bigger number and counting on.

Year 2

Method to be used by core of class

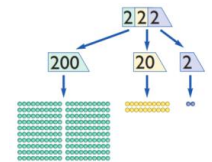
As year 1 plus:

	?
21	34



Addition can be done in any order (commutative)
 $34 + 56$ or $56 + 34$

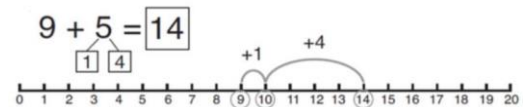
Understand place value - can partition numbers & recombine numbers



$$37 = 30 + 7 \quad 30 + 7 = 37$$

Use partitioning to add numbers, first with concrete apparatus, then as a possible mental method.

Have a range of mental methods for calculating first with numbers to 20, then with numbers to 100 e.g. breaking numbers apart to use them flexibly, this may be with a bridging strategy (e.g. $7 + 5$ could be thought of as $7 + 3 + 2$ or $5 + 5 + 2$), a compensating strategy (e.g. $7 + 9$ could be thought of as $7 + 10$ then -1) or by using a near double (e.g. $7 + 8 = 14 + 1$).



Learn to add three numbers $4 + 7 + 6 = 17$

Put 4 and 6 together to make 10. Add on 7.



$$4 + 7 + 6 = 10 + 7 = 17$$

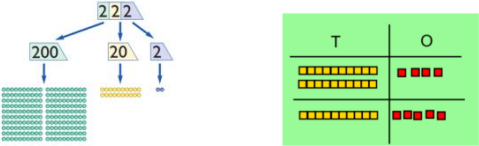
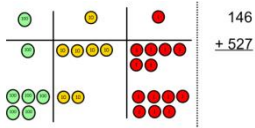
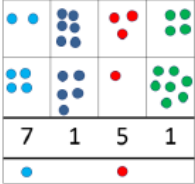
Use number bonds e.g. $4 + 6 = 10$ to work out $40 + 60 = 100$

See addition appendix 2 starting at the bigger number and counting on. Appendix 3 regrouping to make 10. Appendix 4 adding three single digits.

Add Plus Total

+ Addition +

More Sum Altogether

<p>Year 3 Method to be used by core of class</p>	<p>Year 4 Method to be used by core of class</p>	<p>Year 5 Method to be used by core of class</p>	<p>Year 6 Method to be used by core of class</p>
<p>As year 2 plus: Understand place value - can partition numbers & recombine numbers to support column addition.</p>  <p>24 + 15 =</p> <p>Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.</p> <p>Expanded addition, TU then TU crossing tens barriers, then HTU (three digits)</p> $34 + 62 =$ $\begin{array}{r} 30 + 4 \\ \underline{60 + 2} \\ 90 + 6 = 96 \end{array}$  <p>146 +527</p> <p>494 + 368 =</p> $\begin{array}{r} 400 + 90 + 4 \\ \underline{300 + 60 + 8} \\ 700 + 150 + 12 = 862 \end{array}$ <p>then Compact addition</p> $\begin{array}{r} 494 \\ +368 \\ \underline{862} \\ 11 \end{array}$ <p>See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)</p>	<p>As year 3 plus: Add ones, tens, hundreds and thousands to a four-digit number</p>  <p>Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.</p> <p>Compact addition (integers only) with numbers up to four digits</p> <p>e.g.</p> $\begin{array}{r} 7648 \\ +1486 \\ \underline{9134} \\ 111 \end{array}$ <p>Expanded addition may be used for decimals in real contexts e.g. money and length.</p> <p>£11.35+ £12.43=</p> $\begin{array}{r} \text{£}10 + \text{£}1 + 30\text{p} + 5\text{p} + \\ \underline{\text{£}10 + \text{£}2 + 40\text{p} + 3\text{p}} \\ \text{£}20 + \text{£}3 + 70\text{p} + 8\text{p} = \text{£}23.78 \end{array}$ <p>See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)</p>	<p>As year 4 plus: Compact addition with numbers larger than four digits. Compact addition with decimals to two places.</p> <p>e.g.</p> $\begin{array}{r} 32.75 \\ +48.64 \\ \underline{81.39} \\ 11 \end{array}$ $\begin{array}{r} 2 \ 3 \ . \ 3 \ 6 \ 1 \\ 9 \ . \ 0 \ 8 \ 0 \\ + \ 1 \ . \ 3 \ 0 \ 0 \\ \hline 9 \ 3 \ . \ 5 \ 1 \ 1 \\ 2 \ 1 \ 2 \end{array}$ <p>See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)</p>	<p>As year 5 plus: Compact addition involving large numbers. Compact addition with decimals to three places.</p> <p>e.g.</p> $\begin{array}{r} 32.756 \\ +48.646 \\ \underline{81.402} \\ 11 \ 11 \end{array}$ <p>24.5+ 36.238</p> $\begin{array}{r} 24.500 \\ +36.238 \\ \underline{60.738} \\ 1 \end{array}$ <p>See addition appendix 5 column method- no regrouping and appendix 6 column method - regrouping (bridging ten)</p>

Subtract

take away

less than

- Subtraction -

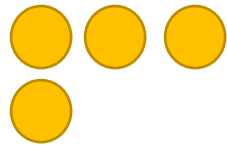
minus

difference between

Year R

Method to be used by core of class

Use physical objects, counters, cubes etc to show how objects can be taken away.



$6 - 2 = 4$



Imagine one less spot



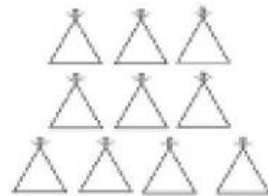
Use counters and bead strings, move them away from the group as you take them away counting backwards as you go.

See subtraction appendix 1 taking away ones and appendix 2 counting back.

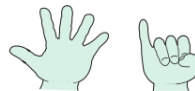
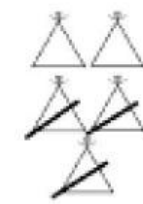
Year 1

Method to be used by core of class

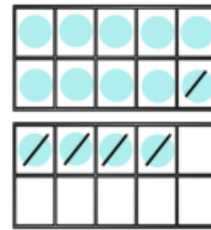
As year R plus:



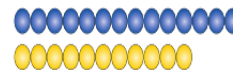
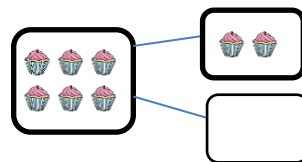
$15 - 3 = 12$



$6 + ? = 10$ $? + 6 = 10$
 $10 - 6 = ?$ $10 - 4 = 6$

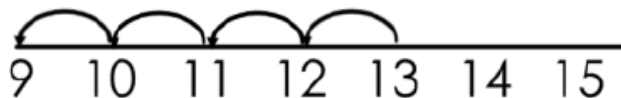


Understand that subtraction can be seen as taking away and finding the difference. Use the part-whole model to take away.



The difference between 11 and 14 is 3.

First with concrete apparatus, then number line or 100 square, then mentally. Count back on a number line or number track when secure with concrete apparatus.



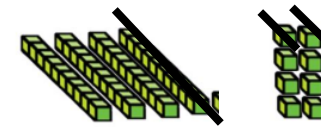
See subtraction appendix 1 taking away ones, appendix 2 counting back, appendix 3 finding the difference and appendix 4 part-whole model.

Year 2

Method to be used by core of class

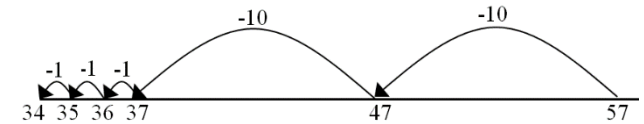
As year 1 plus:

Subtract using concrete objects such as Numicon, make the whole and take away the correct amount. Then progress to pictorial representations and mental methods.



$48 - 12 =$

Start at the bigger number and count back the smaller number showing the jumps on the number line.



This can progress all the way to counting back using two 2 digit numbers.

No. bonds to 100 (at least with multiples of 10). Understand the number line as a continuum. Understand that subtraction is the inverse of addition (Numicon is a particularly useful

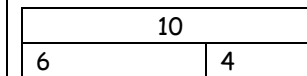
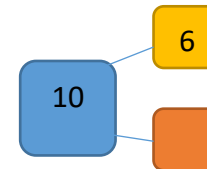
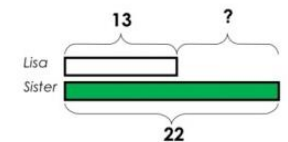


image) and bar model.



See subtraction appendix 2 counting back, appendix 3 finding the difference and appendix 4 part-whole model and appendix 5 make 10.

Subtract

take away

less than

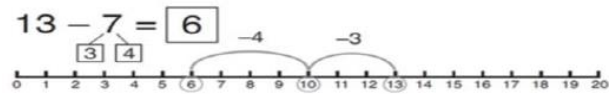
- Subtraction - minus

difference between

Year 3

Method to be used by core of class

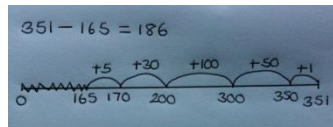
As year 2 plus:



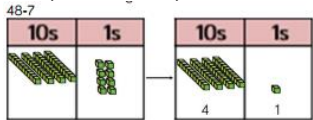
Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.

Number line method (2 and 3 digit numbers)

$$351 - 165 = 186$$



Begin expanded subtraction using concrete objects and pictorial representations.



Start to use Compact subtraction.

Not Regrouping

$$\begin{array}{r} 48 \\ - 7 \\ \hline 41 \end{array}$$

Regrouping

$$\begin{array}{r} 341 \\ - 26 \\ \hline 15 \end{array}$$

Show the carrying at the top as above.

See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

Year 4

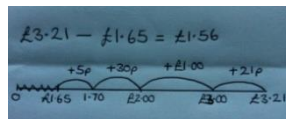
Method to be used by core of class

As year 3 plus:

Subtract ones, tens, hundreds, and thousands from a four-digit number.

Number line method (2, 3, 4 digit numbers, extending to decimals in a real context)

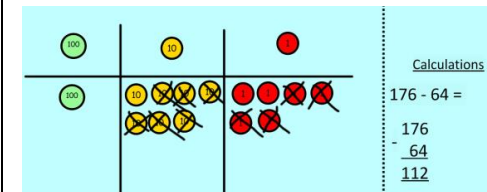
e.g.



Expanded subtraction

$$\text{e.g. } 354 - 165$$

$$\begin{array}{r} 200 \quad 140 \\ 300 + 50 + 1 \\ - 100 + 60 + 5 \\ \hline 100 + 80 + 6 = 186 \end{array}$$



Use base 10 or place value counters alongside the written calculation to help to show working.

Compact subtraction (regrouping)

$$\begin{array}{r} 214 \\ 351 \\ - 165 \\ \hline 186 \end{array}$$

See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

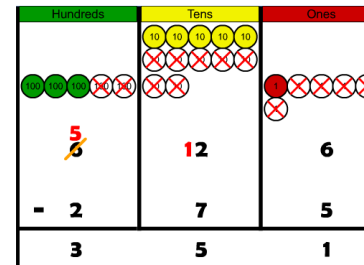
Year 5

Method to be used by core of class

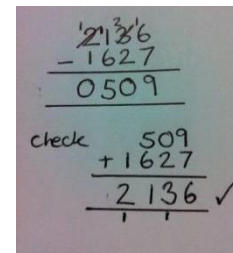
As year 4 plus:

Compact subtraction, involving numbers larger than 4 digits and with decimals to 2 places.

Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident children can find their own way to record the exchange/regrouping.



Compact subtraction, involving numbers larger than 4 digits and with decimals to 2 places. Using the inverse to check.



See Appendix 7 column method with regrouping.

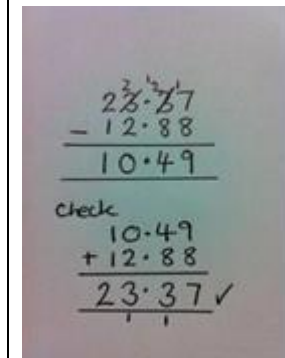
Year 6

Method to be used by core of class

As year 5 plus:

Compact subtraction involving large numbers.

Compact subtraction with decimals up to three places.



See Appendix 7 column method with regrouping.

Multiply times lots of **x Multiplication x** groups of multiple of product

Year R

Method to be used by core of class

Introduce language and concept of making equal groups.
Begin to double numbers to 5. Use concrete apparatus to show how to double a number.

Double 4 is 8



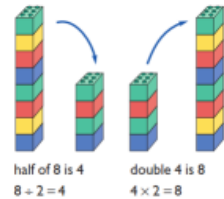
See multiplication appendix 1 doubling.

Year 1

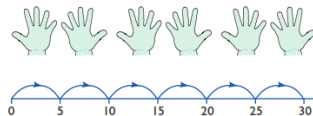
Method to be used by core of class

As year R plus:

Recall doubles to 10. Use this knowledge to support halving and doubling larger numbers.



Understand multiplication as repeated addition.



$5 + 5 + 5 + 5 + 5 + 5 = 30$
 $5 \times 6 = 30$
5 multiplied by 6
6 groups of 5
6 hops of 5



Group sets of objects reliably in 2s, 5s and 10s.



There are ___ groups of ___ pencils.



There are ___ groups of ___ flowers.



Recognise number sequences e.g. 2s, 5s and 10s.

See multiplication appendix 1 doubling. Appendix 2 counting in multiples. Appendix 3 repeated addition. Appendix 4 arrays- showing commutative multiplication.

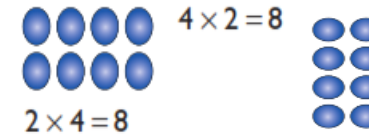
Year 2

Method to be used by core of class

As Year 1 plus:

By the end of the year pupils should recall all multiplication facts for the 2, 5 and 10 times tables.

Understand multiplication is about equal groups and use arrays to show this. Also be able to use these arrays to show and understand that multiplication is commutative.



Understand multiplication as scaling.



The giant is twice as big as a boy.

Understand that multiplication and division are the inverse of each other.

$4 \times 10 = 40$

$10 \times 4 = 40$

$40 \div 4 = 10$

$40 \div 10 = 4$

See multiplication appendix 2 counting in multiples. Appendix 3 repeated addition. Appendix 4 arrays- showing commutative multiplication.

Multiply times lots of **x Multiplication x** groups of multiple of product

Year 3

Method to be used by core of class

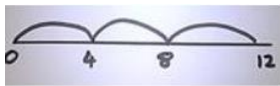
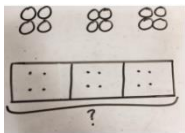
As year 2 plus:

Focus on understanding, representing and remembering times tables facts for 2,5,10,3,4 and 8 times tables, including division facts



$4 \times 8 = 32$, $8 \times 4 = 32$, $32 \div 4 = 8$, $32 \div 8 = 4$

Understand that multiplication is repeated addition e.g. $3 \times 4 = 4 + 4 + 4$. Use concrete, pictorial and abstract methods



Expanded Column & Compact Column Methods

	H	T	O
x	3	4	
+	20		(5 x 4)
	150		(5 x 30)
	170		

	H	T	O
x		3	4
			5
	1	7	0
	1	2	

Note - before moving to any TU x U, the children will need be able to multiply a multiple of 10 by a single digit

See multiplication appendix 4 arrays- showing commutative multiplication. Appendix 5 grid method.

Year 4

Method to be used by core of class

As year 3 plus:

ALL times tables facts to 12×12 should be known by end of year 4 including multiplying by 0 and 1.

Children should learn to multiply three numbers together.

$4 \times 6 \times 3 =$
 $4 \times 6 = 24 \times 3 = 72$

Grid method TU x U or HTU X U This can be used to help children understand exactly what you are multiplying.

e.g. 245×6

x	200	40	5	Tot al
6	120	24	30	147
	0	0	0	0

Partitioning

4×15
 10×5

$10 \times 4 = 40$
 $5 \times 4 = 20$
 $40 + 20 = 60$

Short Multiplication

$6 \times 23 =$
 23
 $\times 6$
 $\hline 138$
1 1

Show the carrying below.

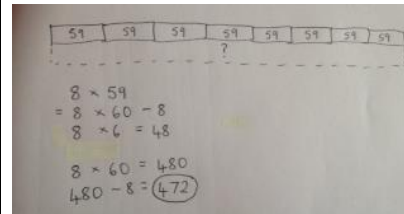
See multiplication appendix 4 arrays- showing commutative multiplication. Appendix 5 grid method.

Year 5

Method to be used by core of class

As year 4 plus:

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written method.



Short multiplication - up to four digits by one digit

2741×6 becomes

2741
 $\times 6$
 $\hline 16446$
4 2

Answer: 16 446

Long Multiplication - four digits by two digits

Use expanded to help understanding if needed then move onto compact.

Expanded

35
 $\times 46$
 $\hline 210$
1400
 $\hline 1610$

Compact

35
 $\times 46$
 $\hline 210$
1400
 $\hline 1610$

See multiplication appendix 4 arrays- showing commutative multiplication. Appendix 5 grid method. Appendix 6 column multiplication.

Year 6

Method to be used by core of class

As year 5 plus:

Long Multiplication

Up to 4 digit x 2 digit

35
 $\times 46$
 $\hline 210$
1400
 $\hline 1610$

Moving to... Decimal numbers to 2 places multiplied by whole numbers

Note -some children may continue to use the grid method

If it helps, children can write out what they are solving next to their answer.

32
 $\times 24$
 $\hline 8$ (4 x 2)
 120 (4 x 30)
 40 (20 x 2)
 600 (20 x 30)
 $\hline 768$

See multiplication appendix 4 arrays- showing commutative multiplication. Appendix 5 grid method. Appendix 6 column multiplication.

Share equally

group equally

divide

÷ **Division** ÷

remainder

factor

quotient

Year R



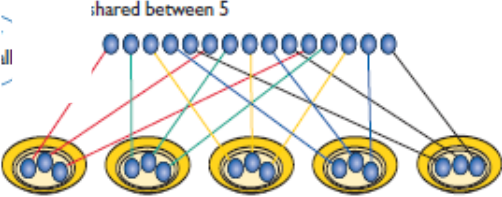

Method to be used by core of class

Introduce language and concept of sharing fairly and making equal groups.

Year 1

Method to be used by core of class

Understand division as sharing equally into groups. Share into groups using concrete apparatus then move to pictorial representations.

☺ ☺ ☺
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* * *
* * *

Finding half and quarter using the same methods.

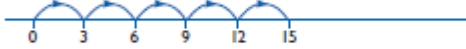
See division appendix 1 sharing objects into groups. Appendix 2 division as grouping. Appendix 3 division within arrays.

Year 2


Method to be used by core of class

As Year 1 plus:


By the end of the year pupils should recall all division facts for the 2, 5 and 10 times tables.



How many 3s in 15?

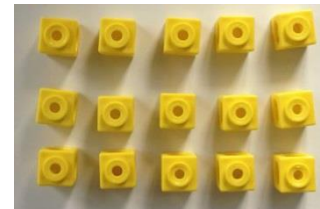


15 ÷ 3 = 5



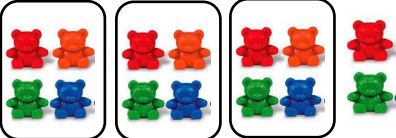

5 hops in 15. How big is each hop?
15 ÷ 5 = 3

Link division to multiplication by creating an array and thinking about the number sentences that can be created.



Eg $15 \div 3 = 5$ $5 \times 3 = 15$
 $15 \div 5 = 3$ $3 \times 5 = 15$

Finding remainders: Divide objects between groups and see how much is left over $14 \div 3 =$

remainder 2

See division appendix 1 sharing objects into groups. Appendix 2 division as grouping. Appendix 3 division within arrays. Appendix 4 division with a remainder.

Share equally

group equally

divide

÷ Division ÷

remainder

factor

quotient

Year 3

Agreed method to be used by core of class

As year 2 plus:

Focus on understanding, representing and remembering times tables facts for 2,5,10,3,4 and 8 times tables, including division facts.

e.g



$4 \times 8 = 32$, $8 \times 4 = 32$, $32 \div 4 = 8$, $32 \div 8 = 4$

Use number lines to support repeated subtraction.

'3 groups of 4, with 1 left over'



See division appendix 3 division within arrays. Appendix 4 division with a remainder.

Year 4

Agreed method to be used by core of class

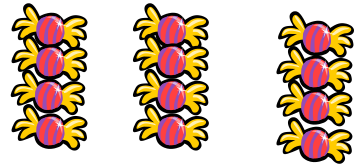
As year 3 plus:

Focus on understanding, representing and remembering times tables facts for ALL times tables up to 12 x12 including division facts.

It is especially important that children understand that division can be grouping or sharing.

e.g. $12 \div 3 = 4$

12 sweets between 3 people gives 4 sweets each.



(3 groups of 4)

'How many 3s in 12?' gives 4 groups of 3

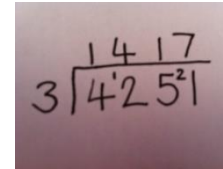
See division appendix 3 division within arrays. Appendix 4 division with a remainder.

Year 5

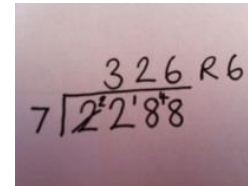
Agreed method to be used by core of class

As year 4 plus:

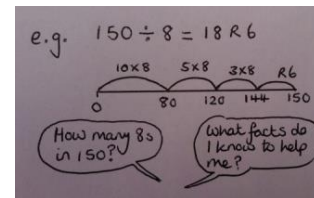
Short division, up to 4 digit numbers divided by 1 digit numbers e.g. $4251 \div 3$



Including dealing with remainders in context.



Or...Chunking on a number line to aid less able children.



Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.

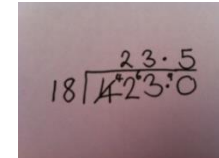
See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division.

Year 6

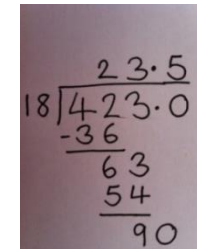
Agreed method to be used by core of class

As year 5 plus:

Short division, up to 4 digit numbers divided by 1 or 2 digit numbers e.g. $423 \div 18$



or Long division

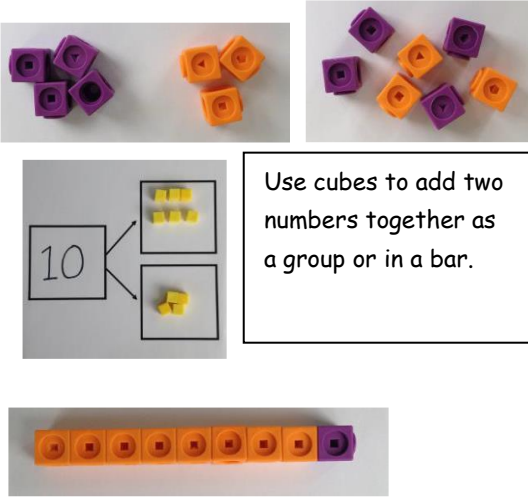
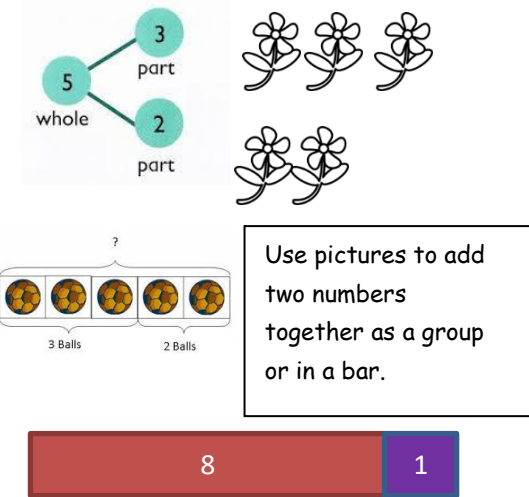
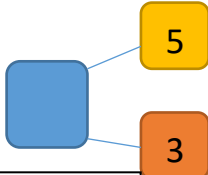

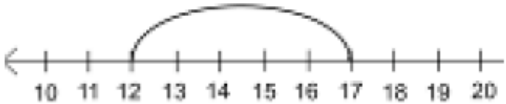


See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division, Appendix 6 long division.

Appendix

Progression in calculations linked to concrete apparatus, pictorial representations and abstract methods. When introducing a new method of calculation the concrete apparatus should be used first. Once this is secure pupils can then be moved onto pictorial representations and then abstract methods.

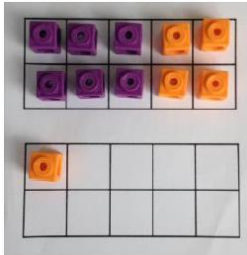
Addition:

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Appendix 1- Combining two parts to make a whole: part-whole model</p>	 <p>Use cubes to add two numbers together as a group or in a bar.</p>	 <p>Use pictures to add two numbers together as a group or in a bar.</p>	<p>$4 + 3 = 7$ $10 = 6 + 4$</p>  <p>Use the part-part whole diagram as shown above to move into the abstract.</p>
<p>Appendix 2- Starting at the bigger number and counting on</p>	 <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p>	<p>$12 + 5 = 17$</p>  <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p>	<p>$5 + 12 = 17$</p> <p>Place the larger number in your head and count on the smaller number to find your answer.</p>

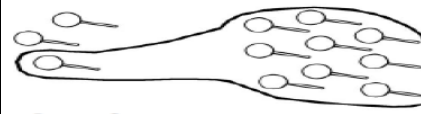
Appendix 3-
Regrouping to make 10.



$$6 + 5 = 11$$

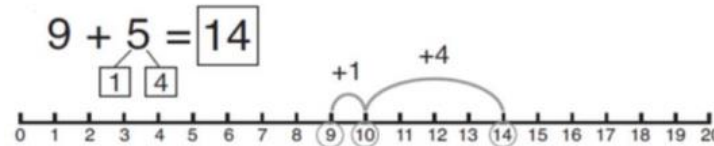


Start with the bigger number and use the smaller number to make 10.



$$3 + 9 =$$

Use pictures or a number line. Regroup or partition the smaller number to make 10.



$$7 + 4 = 11$$

If I am at seven, how many more do I need to make 10. How many more do I add on now?

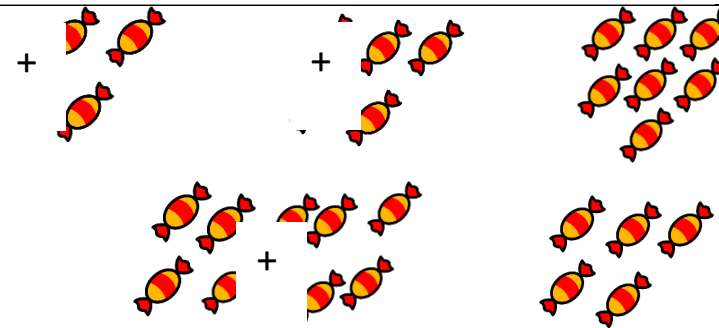
Appendix 4-
Adding three single digits

$$4 + 7 + 6 = 17$$

Put 4 and 6 together to make 10. Add on 7.



Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.



Add together three groups of objects. Draw a picture to recombine the groups to make 10.

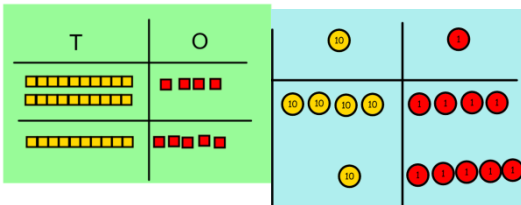
$$\begin{aligned} (4) + 7 + (6) &= 10 + 7 \\ 10 & \\ &= 17 \end{aligned}$$

Combine the two numbers that make 10 and then add on the remainder.

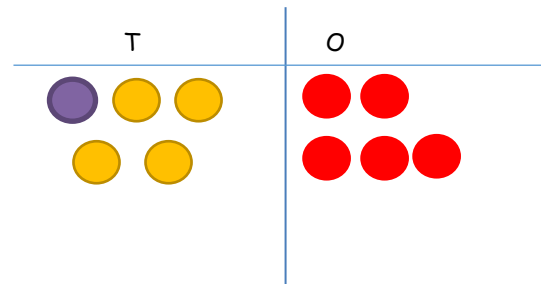
Appendix 5-
Column method- no regrouping

$$24 + 15 =$$

Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.



After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.



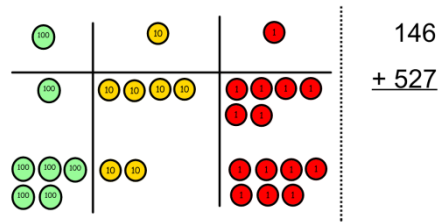
Calculations

$$21 + 42 =$$

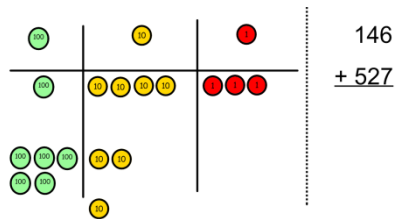
$$\begin{array}{r} 21 \\ + 42 \\ \hline \end{array}$$

Appendix 6-
Column method-
regrouping (bridging 10)

Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10.

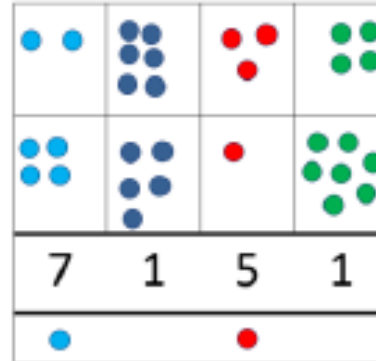


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

$$\begin{array}{r} 20 + 5 \\ 40 + 8 \\ 60 + 13 = 73 \end{array}$$

$$\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$$

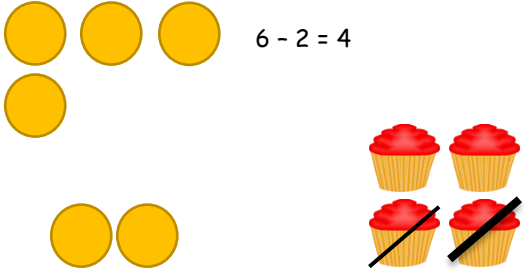
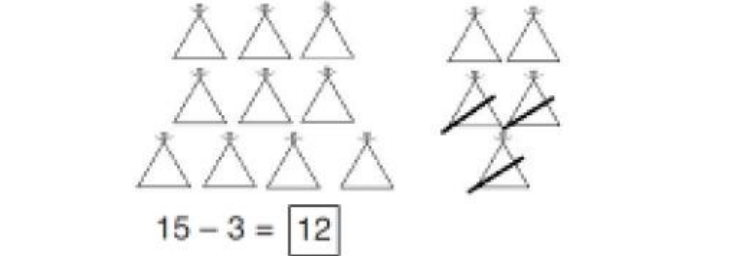


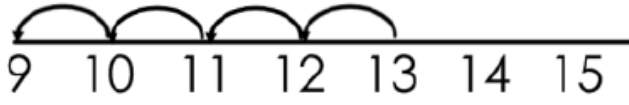
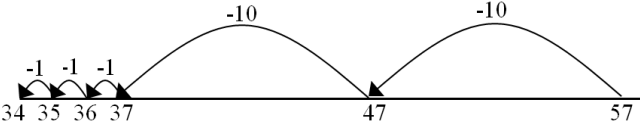
As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

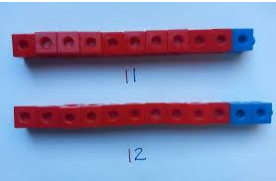
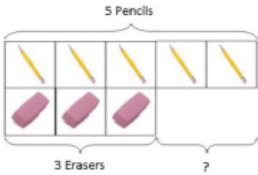
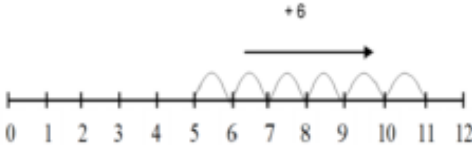
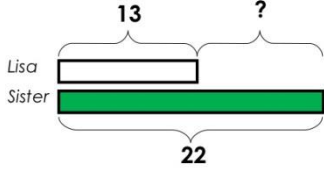
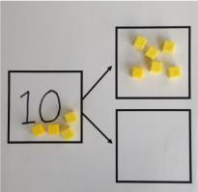
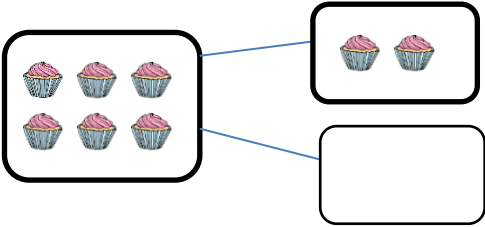
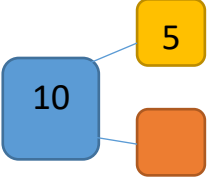

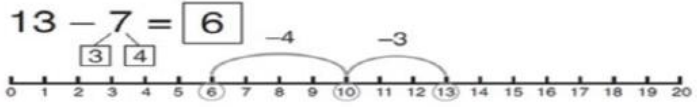
$$\begin{array}{r} 72.8 \\ + 54.6 \\ \hline 127.4 \end{array}$$

$$\begin{array}{r} \pounds 23.59 \\ + \pounds 7.55 \\ \hline \pounds 31.14 \\ \small 1 \quad 1 \quad 1 \end{array}$$

$$\begin{array}{r} 23.361 \\ 9.080 \\ 59.770 \\ + 1.300 \\ \hline 93.511 \\ \small 2 \quad 1 \quad 2 \end{array}$$

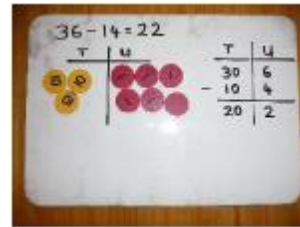
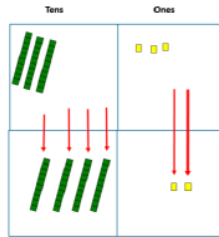
Subtraction:

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Appendix 1- Taking away ones</p>	<p>Use physical objects, counters, cubes etc to show how objects can be taken away.</p>  <p>$6 - 2 = 4$</p>	<p>Cross out drawn objects to show what has been taken away.</p>  <p>$15 - 3 = 12$</p>	<p>$18 - 3 = 15$</p> <p>$8 - 2 = 6$</p>
<p>Appendix 2- Counting back</p>	<p>Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.</p>  <p>$13 - 4$</p> <p>Use counters and move them away from the group as you take them away counting backwards as you go.</p> 	<p>Count back on a number line or number track</p>  <p>$9 \quad 10 \quad 11 \quad 12 \quad 13 \quad 14 \quad 15$</p> <p>Start at the bigger number and count back the smaller number showing the jumps on the number line.</p>  <p>$34 \quad 35 \quad 36 \quad 37 \quad 47 \quad 57$</p> <p>This can progress all the way to counting back using two 2 digit numbers.</p>	<p>Put 13 in your head, count back 4. What number are you at? Use your fingers to help.</p>

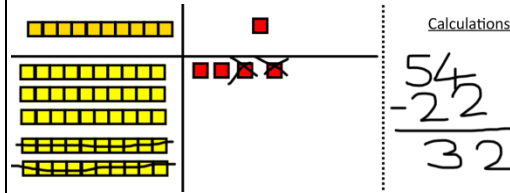
<p>Appendix 3- Find the difference</p>	<p>Compare amounts and objects to find the difference.</p>  <p>Use cubes to build towers or make bars to find the difference</p>  <p>Use basic bar models with items to find the difference</p>	 <p>Count on to find the difference.</p> <p>Comparison Bar Models</p> <p>Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.</p>  <p>Draw bars to find the difference between 2 numbers.</p>	<p>Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.</p>
<p>Appendix 4 Part- Whole Model</p>	 <p>Link to addition- use the part whole model to help explain the inverse between addition and subtraction.</p> <p>If 10 is the whole and 6 is one of the parts. What is the other part?</p> <p>$10 - 6 =$</p>	<p>Use a pictorial representation of objects to show the part part whole model.</p> 	 <p>Move to using numbers within the part whole model.</p>
<p>Appendix 5- Make 10</p>	<p>$14 - 9 =$</p>  <p>Make 14 on the ten frame. Take away the four first to make 10 and then take away one more so you have taken away 5. You are left with the answer of 9.</p>	<p>$13 - 7 = 6$</p>  <p>Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.</p>	<p>$16 - 8 =$</p> <p>How many do we take off to reach the next 10?</p> <p>How many do we have left to take off?</p>

Appendix 6-
Column method without regrouping

Use Base 10 to make the bigger number then take the smaller number away.



Show how you partition numbers to subtract. Again make the larger number first.



Calculations

$$\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$$

Draw the Base 10 or place value counters alongside the written calculation to help to show working.

$$47 - 24 = 23$$

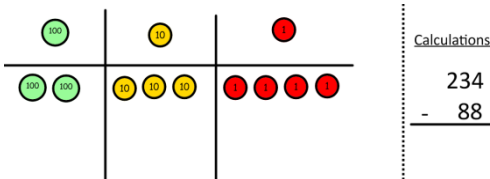
$$\begin{array}{r} 40 + 7 \\ - 20 + 4 \\ \hline 20 + 3 \end{array}$$

This will lead to a clear written column subtraction.

Appendix 7-
Column method with regrouping

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

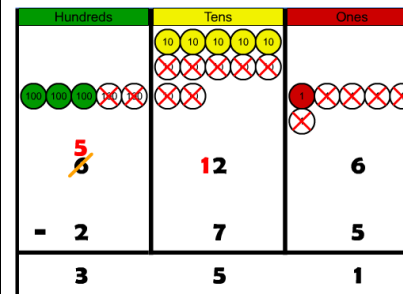
Make the larger number with the place value counters



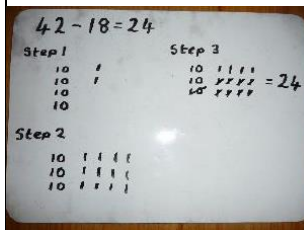
Calculations

$$\begin{array}{r} 234 \\ - 88 \\ \hline \end{array}$$

Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



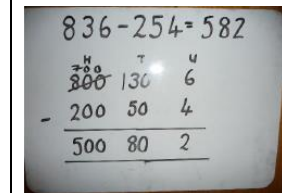
Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



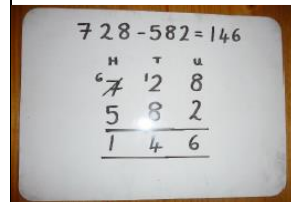
When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows

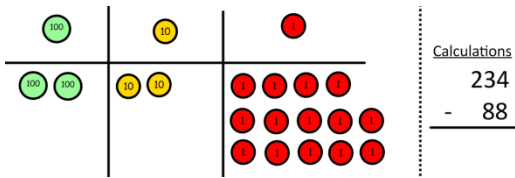
when to exchange/regroup.



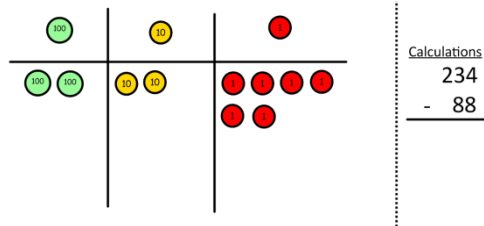
Children can start their formal written method by partitioning the number into clear place value columns.



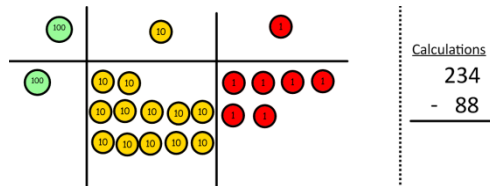
Moving forward the children use a more compact method.



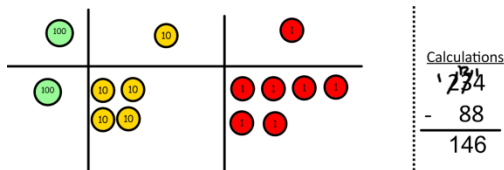
Now I can subtract my ones.



Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

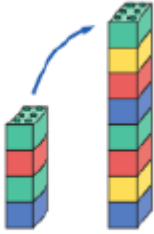

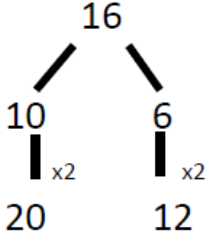
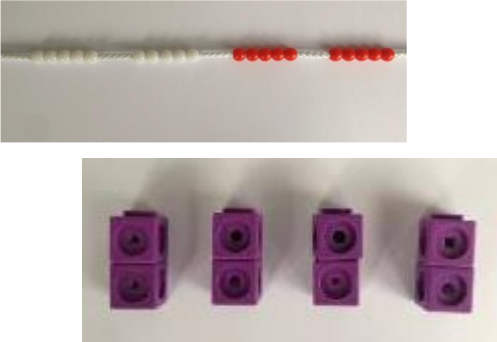
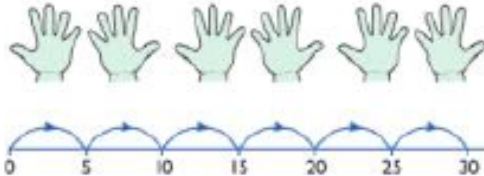


Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

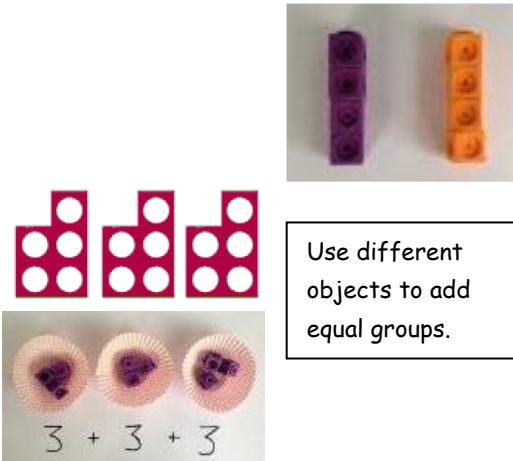
This will lead to an understanding of subtracting any number including decimals.

$$\begin{array}{r} 5 \quad 12 \quad 1 \\ 2 \quad \cancel{6} \quad \cancel{3} \quad . \quad \color{red}{0} \\ - \quad 2 \quad 6 \quad . \quad 5 \\ \hline 2 \quad 3 \quad 6 \quad . \quad 5 \end{array}$$

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Appendix 1- Doubling</p>	<p>Use practical activities to show how to double a number.</p>  <p>double 4 is 8 $4 \times 2 = 8$</p>	<p>Draw pictures to show how to double a number.</p> <p>Double 4 is 8</p> 	 <p>Partition a number and then double each part before recombining it back together.</p>
<p>Appendix 2- Counting in multiples</p>	 <p>Count in multiples supported by concrete objects in equal groups.</p>	 <p>Use a number line or pictures to continue support in counting in multiples.</p>	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>

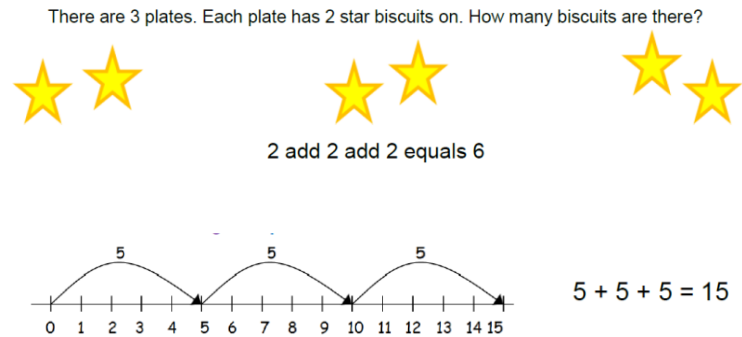
Appendix 3-
Repeated addition



Use different objects to add equal groups.

$$3 + 3 + 3$$

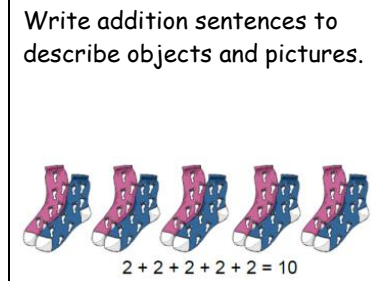
There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?



2 add 2 add 2 equals 6

$$5 + 5 + 5 = 15$$

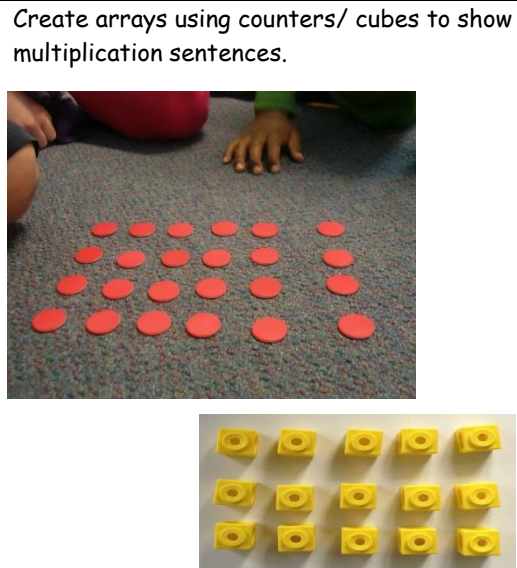
Write addition sentences to describe objects and pictures.



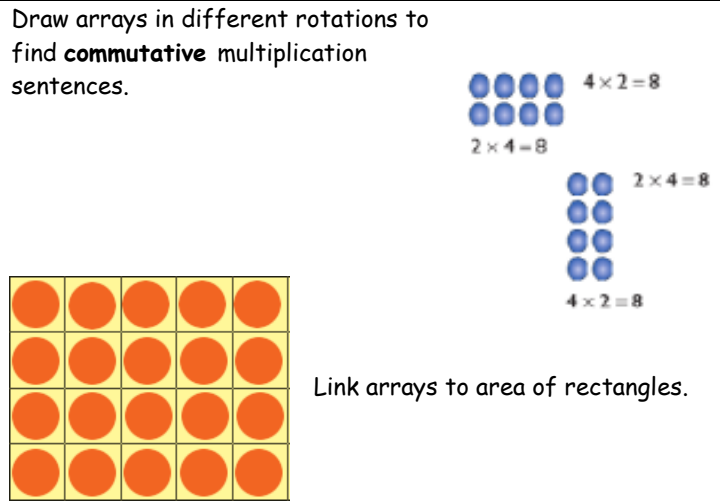
$$2 + 2 + 2 + 2 + 2 = 10$$

Appendix 4-
Arrays- showing commutative multiplication

Create arrays using counters/ cubes to show multiplication sentences.



Draw arrays in different rotations to find **commutative** multiplication sentences.



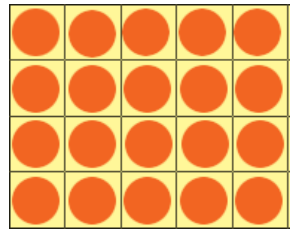
$$4 \times 2 = 8$$

$$2 \times 4 = 8$$

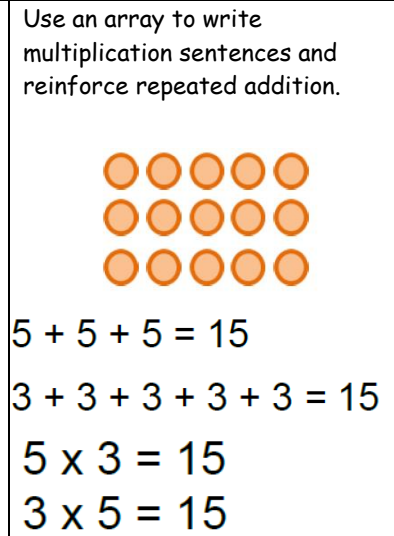
$$2 \times 4 = 8$$

$$4 \times 2 = 8$$

Link arrays to area of rectangles.



Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

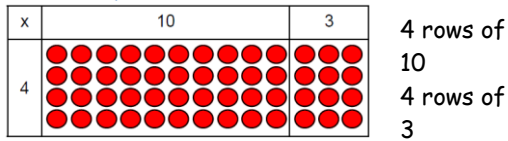
$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

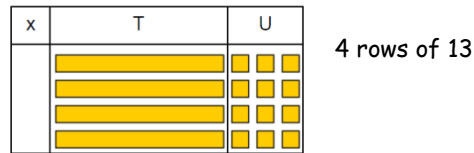
$$3 \times 5 = 15$$

Appendix 5-
Grid Method

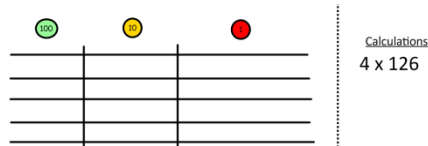
Show the link with arrays to first introduce the grid method.



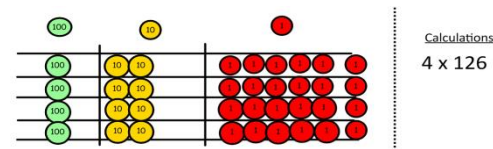
Move on to using Base 10 to move towards a more compact method.



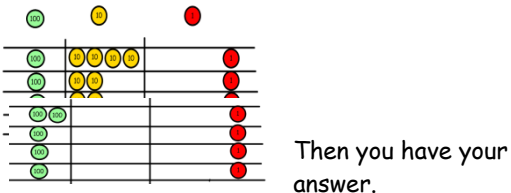
Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.

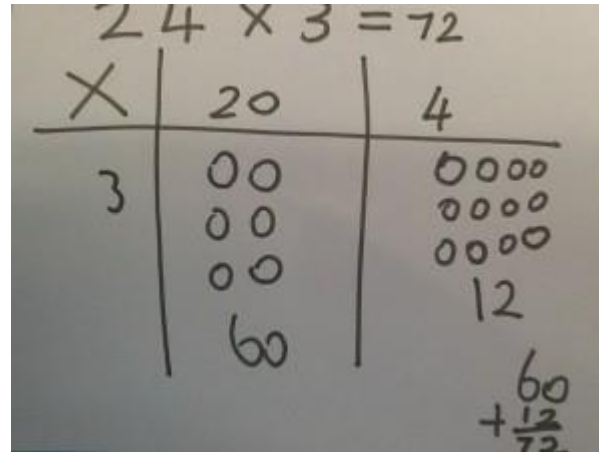


Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

x	30	5
7	210	35

$$210 + 35 = 245$$

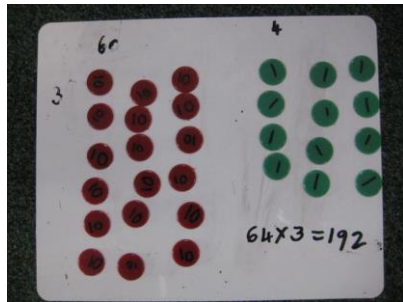
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

	10	8
10	100	80
3	30	24

x	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

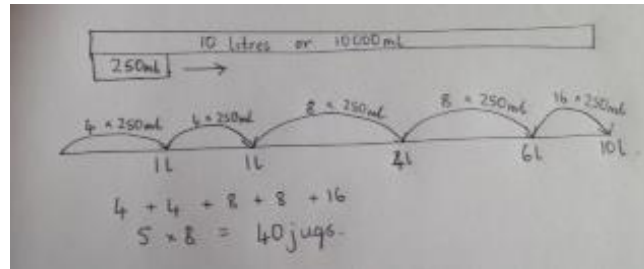
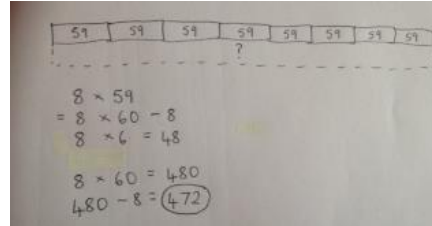
Appendix 6-
Column multiplication

Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.



Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.


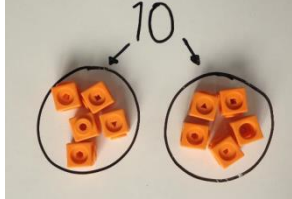

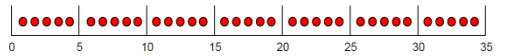
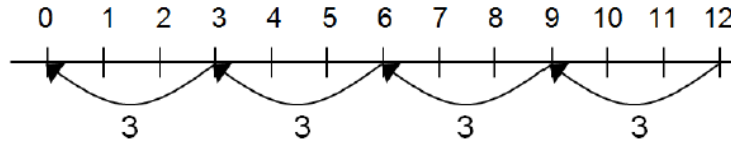
$$\begin{array}{r}
 32 \\
 \times 24 \\
 \hline
 8 \quad (4 \times 2) \\
 120 \quad (4 \times 30) \\
 40 \quad (20 \times 2) \\
 600 \quad (20 \times 30) \\
 \hline
 768
 \end{array}$$

$$\begin{array}{r}
 7 \ 4 \\
 \times 6 \ 3 \\
 \hline
 1 \ 2 \\
 2 \ 1 \ 0 \\
 2 \ 4 \ 0 \\
 + 4 \ 2 \ 0 \ 0 \\
 \hline
 4 \ 6 \ 6 \ 2
 \end{array}$$

This moves to the more compact method.

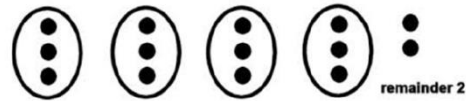
$$\begin{array}{r}
 2 \ 3 \ 1 \\
 1 \ 3 \ 4 \ 2 \\
 \times 1 \ 8 \\
 \hline
 1 \ 3 \ 4 \ 2 \ 0 \\
 1 \ 0 \ 7 \ 3 \ 6 \\
 \hline
 2 \ 4 \ 1 \ 5 \ 6 \\
 1
 \end{array}$$

Division

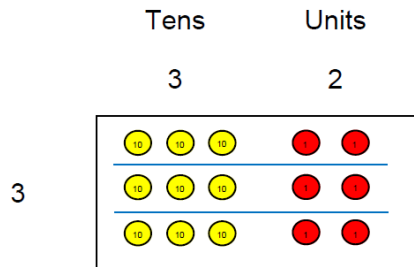
Objective and Strategies	Concrete	Pictorial	Abstract
<p>Appendix 1- Sharing objects into groups</p>	 <p>I have 10 cubes, can you share them equally in 2 groups?</p> 	<p>Children use pictures or shapes to share quantities.</p>  <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> $8 \div 2 = 4$ </div>	<p>Share 9 buns between three people.</p> $9 \div 3 = 3$
<p>Appendix 2- Division as grouping</p>	<p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p> 	<p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p> 	$28 \div 7 = 4$ <p>Divide 28 into 7 groups. How many are in each group?</p>



Draw dots and group them to divide an amount and clearly show a remainder.



Appendix 5-
Short division



Use place value counters to divide using the bus stop method alongside



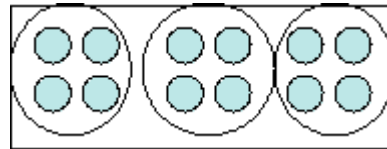
Calculations
 $42 \div 3$



$42 \div 3 =$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

Move onto divisions with a

$$\begin{array}{r} 218 \\ \hline \end{array}$$

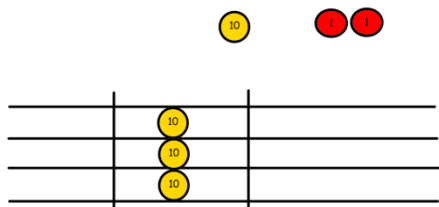
$$\begin{array}{r} 86r2 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ \hline 5 \overline{) 432} \end{array}$$

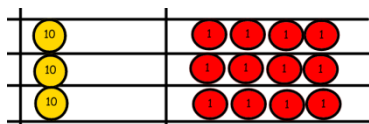
remainder.

Finally move into decimal places to divide the total accurately.

$$\begin{array}{r} 14.6 \\ \hline 35 \overline{) 511.0} \end{array}$$



We exchange this ten for ten ones and then share the ones equally among the groups.



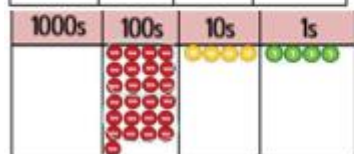
We look how much in 1 group so the answer is 14.

Appendix 6 - Long Division

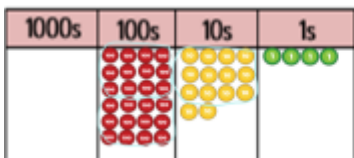
Using Place Value Counters
2544 ÷ 12



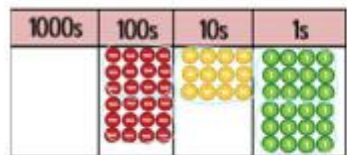
We can't group 2 thousands into groups of 12 so will exchange them.



We can group 24 hundreds into groups of 12 which leaves with 1 hundred.



After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12, which leaves 2 tens.



After exchanging the 2 tens, we have 24 ones. We can group 24 ones into 2 group of 12, which leaves no remainder.

Abstract

$$\begin{array}{r} 02 \\ 12 \overline{) 2544} \\ \underline{24} \\ 1 \end{array}$$

$$\begin{array}{r} 021 \\ 12 \overline{) 2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 2 \end{array}$$

$$\begin{array}{r} 0212 \\ 12 \overline{) 2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$$

